

**MAT 254 – Winter Quarter 2002**  
**Test 4**

NAME \_\_\_\_\_

**Show work and write clearly.**

**Make sure graphs show approximating rectangle,  $R(x)$ ,  $r(x)$ ,  $p(x)$  and  $h(x)$ .**

1. (30 pts.) Use the disk method to find the volume of the solid obtained by rotating the region bounded by  $x = y - y^2$  and  $x = y^2 - 3$  about  $x = -4$ .

2. (30 pts.) Find the following integrals:

a.  $\int (\tan^{-1} x) dx$

b.  $\int (x^4 \ln x) dx$

c.  $\int_0^1 (x^3 e^{x^2}) dx$

3. (30 pts.) Use the shell method to find the volume of the solid obtained by rotating the region bounded by  $y = x^2$ ,  $y = 1$  and  $x = 2$  about  $y = -3$ .

4. (10 pts.) Solve:  $y' = \frac{xy}{3 \ln y}$ .